(Hyper)Property-Preserving Compilers

summer semester 18-19, block



Marco Patrignani^{1,2}



Properties and Hyperproperties

- Formalise any security property
- Established theory with practical applications
- Recommended reading:
 - Schneider. 2000. Enforceable security policies.
 - Alpern and Schneider. 1985. Defining liveness.
 - Clarkson and Schneider. 2010. Hyperproperties.

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- trace t = sequence of (formalised as \overline{sth})
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 - component-context interactions α ? α !...
 - code-environment interaction *read* v; write v
 We use t abstractly now, though mostly:

 $t = \overline{\Theta}$

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- This is **unlike** program equivalence:
 - properties talk a single program

Examples

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 ⊢ readΘ and ⊢ sendΘ' are abstract predicates
- GS: $\{t \mid \vdash req\Theta_i \Rightarrow \vdash resp\Theta_j \text{ where } j > i\}$ GS: the program eventually responds to the requests

Properties are partitioned in

 Safety: something bad does not happen (NRW) Properties are partitioned in

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- Liveness: something good eventually happens (GS)



• Safety = integrity



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- but, Safety = weak secrecy: we don't leak a fresh k to €

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- In the following: m is a finite trace t (a finite $\overline{\Theta}$) aka a prefix
- NRW-dual:

 $\{m \mid \Theta < \Theta'. \vdash read \Theta \land \vdash send \Theta'\}$

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- capture a single run (the trace) of any program (the set)
 Hyperproperties = sets of sets of traces
- capture multiple runs (the *sets of traces*) of any program (the sets)

Example: NonInterference

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- high = secret, low = public
- a set of traces tells all the behaviours of the same program with different high inputs

$$\begin{cases} \mathsf{NI}: \\ \left\{ t_1, t_2 \right\} & \text{if inputs } (t_1) =_L \texttt{inputs } (t_2) \\ & \text{then outputs } (t_1) =_L \texttt{outputs } (t_2) \end{cases} \end{cases}$$

Example: Average Response Time < 1

ART:

$$\left\{ \{t \cdots\} \mid \text{mean}\left(\bigcup_{t \in \{t \cdots\}} \text{response_time}(t) \right) < 1 \right\}$$
where response_time(·) looks in trace t and
checks time between req(·) and resp(·)

Hypersafety and Hyperliveness

Like Properties, Hyperproperties are partitioned in

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NI-dual:

\begin{cases} \{t_1, t_2\} & \text{ if inputs } (t_1) =_L \text{ inputs } (t_2) \\ & \text{ then outputs } (t_1) \neq_L \text{ outputs } (t_2) \end{cases}
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- $\vdash P : \pi \stackrel{\text{\tiny def}}{=} \text{ if } P \rightsquigarrow t \text{ then } t \in \pi$

Hyperproperty Satisfaction

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So we want our program P to satisfy NRW, GS, NI or ART: $\forall \mathfrak{C}.\mathfrak{C}[P]$, so $\Theta = \mathfrak{C}[P]$

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So we want our program P to satisfy NRW, GS, NI or ART: $\forall \mathfrak{C}.\mathfrak{C}[P]$, so $\Theta = \mathfrak{C}[P]$

Reminiscent of contextual equivalence!

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- we must filter events and consider only those generated by *P*

Example: Robust Safety

- $\pi \in Safety$
- $\vdash_R P : \pi \stackrel{\text{\tiny def}}{=} \forall \mathfrak{C}. \text{ if } \mathfrak{C}[P] \rightsquigarrow t \text{ then } t \in \pi$

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- dually: $\{m\} :: \pi \in Safety$
- $m \le t$ = m is a prefix of t
- $\vdash_R P : \{m\} \stackrel{\text{\tiny def}}{=} \forall \mathfrak{C}. \text{ if } \mathfrak{C}[P] \rightsquigarrow t \text{ then } \nexists m \in \{m\}.m \leq t$

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- we need a fair context in our setup: a context that will interact with us
- avoid DOS: the attacker wants to violate our code, not starve it

1. specify (hyper)properties on programs through traces

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- 2. specify (hyper)properties robustly

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Q: can we preserve them through compilation?

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Q: can we preserve them through compilation?

Yes!

Assumptions

- same alphabet of traces between S and T (I/O or syscalls)
- we lift this (partially) later

Example: Robust Property Preservation

• Assume the source has a property robustly

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$$RTP: \forall \pi. \ \forall \mathsf{P}. \ (\forall \mathfrak{C} \ t. \mathfrak{C}[\mathsf{P}] \rightsquigarrow t \Rightarrow t \in \pi) \Rightarrow$$
$$(\forall \mathfrak{C} \ t. \mathfrak{C}[[\mathsf{P}]] \rightsquigarrow t \Rightarrow t \in \pi)$$

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Correct definitions



Correct definitions

Hard to use: no proof support
Evaluation

Correct definitions

Hard to use: no proof support We want equivalent criteria that are easy to prove

Example: Robust Property Preservation #2

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 $PFRTP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall t. \ \mathfrak{C}[\llbracket\mathsf{P}]] \rightsquigarrow t \Rightarrow$ $\exists \mathfrak{C}. \mathfrak{C}[\mathsf{P}] \rightsquigarrow t$

RTP Intuition

If any trace in the target is also done in the source, and the source has the property, so does the target.

Example: Robust Safety Preservation #2

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Example: Robust Safety Preservation #2

 $PFRSP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall m.$ $\mathfrak{C}[\llbracket \mathsf{P} \rrbracket] \rightsquigarrow m \Longrightarrow$ $\exists \mathfrak{C}. \ \mathfrak{C}[\mathsf{P}] \rightsquigarrow m$

27/40

Safety is defined **dually** as a set of bad prefixes If any prefix done in the target is also done in the source and the source has the safety property, that prefix is not bad, so the target also has the safety property

• $RTP \iff PFRTP$

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 $RHP: \forall H. \forall \mathsf{P}. (\forall \mathfrak{C}. \operatorname{Behav} (\mathfrak{C}[\mathsf{P}]) \in H) \Rightarrow (\forall \mathfrak{C}. \operatorname{Behav} (\mathfrak{C}[[\mathsf{P}]]) \in H)$

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 $PFRHP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \exists \mathfrak{C}. \ \mathsf{Behav}\left(\mathfrak{C}[\llbracket\mathsf{P}\rrbracket]\right) = \mathsf{Behav}\left(\mathfrak{C}[\mathsf{P}]\right)$ $PFRHP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \exists \mathfrak{C}. \ \forall t. \ \mathfrak{C}[\llbracket\mathsf{P}\rrbracket] \rightarrow t \iff \mathfrak{C}[\mathsf{P}] \sim t$

Quiz: Spot the Differences

$PFRTP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall t. \ \mathfrak{C}[\llbracket \mathsf{P} \rrbracket] \rightsquigarrow t \Rightarrow \exists \ \mathfrak{C}. \ \mathfrak{C}[\mathsf{P}] \rightsquigarrow t$

$PFRHP : \forall \mathsf{P}. \forall \mathfrak{C}. \exists \mathfrak{C}. \forall t. \mathfrak{C}[[\mathsf{P}]] \rightarrow t \iff \mathfrak{C}[\mathsf{P}] \rightarrow t$



Quantifier ordering

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- Quantifier ordering: lifts to sets of traces since a *c* in PFRHP works for a set of traces
- Implication: a single implication means refinement, so the target can have more behaviours. Co-implication means no refinement, we need the exact same traces to ensure inclusion in the H 33/40

Example: Robust Hypersafety Preservation

$\begin{aligned} PFRHSP: \ \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall \{m\}.\\ \{m\} \leq \operatorname{Behav}\left(\mathfrak{C}[\llbracket \mathsf{P} \rrbracket]\right) \Rightarrow \exists \mathfrak{C}. \ \{m\} \leq \operatorname{Behav}\left(\mathfrak{C}[\mathsf{P}]\right) \end{aligned}$

Example: Robust Hypersafety Preservation

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Where \leq means *all* prefixes of $\{m\}$ are extended by the behaviour of the (compiled) program

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- Hyperliveness: not present: RHLP collapses with RHP

Robust Compilation (RC) Diagram



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RC vs FAC

• (some) RC criteria are propositional

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RC vs FAC

- (some) RC criteria are propositional (some are relational but they are not presented here)
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- both are robust
- FAC is only as precise as the equivalence
- RC do not preserve abstractions beyond the related security (hyper)property

Proving RC

 $\begin{aligned} PFRTP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall t. \\ & \mathfrak{C}[\llbracket \mathsf{P} \rrbracket] \rightsquigarrow t \Rightarrow \exists \mathfrak{C}. \mathfrak{C}[\mathsf{P}] \rightsquigarrow t \\ PFRSP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall m. \\ & \mathfrak{C}[\llbracket \mathsf{P} \rrbracket] \rightsquigarrow m \Rightarrow \exists \mathfrak{C}. \mathfrak{C}[\mathsf{P}] \rightsquigarrow m \end{aligned}$

Proving RC

 $PFRTP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall t.$ $\mathfrak{C}[\llbracket \mathsf{P} \rrbracket] \rightsquigarrow t \Rightarrow \exists \mathfrak{C}. \mathfrak{C}[\mathsf{P}] \rightsquigarrow t$ $PFRSP : \forall \mathsf{P}. \ \forall \mathfrak{C}. \ \forall m.$ $\mathfrak{C}[\llbracket \mathsf{P} \rrbracket] \rightsquigarrow m \Rightarrow \exists \mathfrak{C}. \mathfrak{C}[\mathsf{P}] \rightsquigarrow m$ $Recall \Rightarrow \text{ for FAC (contrapositive):}$

Proving RC

 $PFRTP: \forall \mathsf{P}. \forall \mathfrak{C}. \forall t.$ $\mathfrak{C}[[\mathsf{P}]] \rightarrow t \Rightarrow \exists \mathfrak{C}.\mathfrak{C}[\mathsf{P}] \rightarrow t$ $PFRSP: \forall \mathsf{P}. \forall \mathfrak{C}. \forall m.$ $\mathfrak{C}[[P]] \rightarrow m \Rightarrow \exists \mathfrak{C} \, \mathfrak{C}[P] \rightarrow m$ Recall \Rightarrow for FAC (contrapositive): $\forall P_1, P_2$ $\exists \mathfrak{C}.\mathfrak{C}[\llbracket \mathsf{P}_1 \rrbracket] \uparrow \iff \mathfrak{C}[\llbracket \mathsf{P}_2 \rrbracket] \Rightarrow \exists \mathfrak{C}.\mathfrak{C}[\mathsf{P}_1 \rbrack \uparrow \iff \mathfrak{C}[\mathsf{P}_2 \rbrack \uparrow$

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- BT is not the inverse of compilation

Conclusion

We have seen:

- Properties and Hyperproperties: to formalise a program having a securty property
- Robust compilation criteria, which preserve classes of (hyper)properties
- Backtranslation-equivalent Robust compilation criteria