Synthesizing Structured CAD Models with Equality Saturation and Inverse Transformations

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Abstract
Recent program synthesis techniques help users customize CAD models (e.g., for 3D printing) by decompiling low-level triangle meshes to Constructive Solid Geometry (CSG) expressions. Without loops or functions, editing CSG can require many coordinated changes, and existing mesh decoders use heuristics that can obfuscate high-level structure.

This paper proposes a second decompilation stage to robustly “shrink” unstructured CSG expressions into more editable programs with map and fold operators. We present Szalinski, a tool that uses Equality Saturation with semantics-preserving CAD rewrites to efficiently search for smaller equivalent programs. Szalinski relies on inverse transformations, a novel way for solvers to speculatively add equivalences to an E-graph. We qualitatively evaluate Szalinski in case studies, show how it composes with an existing mesh decoder, and demonstrate that Szalinski can shrink large models in seconds.

1 Introduction
The programming languages and machine learning communities have developed techniques to decompile Computer-Aided Design (CAD) models from low-level numerical representations to Constructive Solid Geometry (CSG) expressions [11, 13, 14, 21, 30, 31, 36]. These techniques aim to help users modify designs shared in online repositories [1, 15, 35].

Recent program synthesis results [11, 21] decompile meshes, sets of triangles defining an object’s surface, into equivalent CSG expressions. CSG includes geometric primitives like cylinders, affine transformations like translate, and set theoretic operators like union.

Existing mesh decoders synthesize flat output: CSG has no loops or functions (Figure 1, left). Therefore, CSG synthesized from large meshes with repetitive features also tends to be large and repetitive. As in traditional programming, repetition makes otherwise intuitive edits tedious and error-prone.

Mesh decompilation is under-constrained [11, 21], so past tools rely on heuristics which cause them to exhibit two challenging features: (C1) synthesize equivalent but dissimilar CSG expressions for the same feature repeated under different transformations, and (C2) arbitrarily order CSG
This paper proposes a second decimation stage that composes with prior work: given a flat CSG expression, produce an equivalent, smaller, and more editable program with map and fold operators for expressing repetition. We present \textit{Szalinski} (Figure 1), a tool which combines semantics-preserving rewrites with simple solvers to synthesize structured CAD programs in a language called \textit{Caddy}.

Szalinski is designed to robustly handle the noisy and unstructured outputs of existing mesh decimers. In many of these outputs, high-level structure is only apparent after a set of CAD-specific rewrites have been judiciously applied (C1). Past work on Equality Saturation [34] suggests that Equality Graphs (E-graphs) [22]—an efficient data structure underlying SMT solvers [8, 10] and program optimizers [16, 33, 34, 42]—would make a good fit for Szalinski because E-graphs can compactly encode many of the equivalent ways to express a program with respect to a set of rewrites.

Unfortunately, reordering with associative and commutative rewrites can cause E-graphs to blow up exponentially. This is known as the \textit{AC-matching problem} [3, 6, 17]. It presents a significant challenge for Szalinski because existing mesh decimers typically output CSG features ordered by heuristics (e.g., geometric proximity) rather than high-level structure (C2).

To address the AC-matching problem in Szalinski we present \textit{inverse transformations}, a novel way for solvers to \textit{speculatively} unify expressions in an E-graph which would be equivalent modulo reordering or partitioning. Before unifying a result \( R \) with its input \( I \), a solver can annotate \( R \) with an inverse transformation which encodes how it manipulated \( I \) to find the more-profitable \( R \). Szalinski then uses syntactic rewrites to \textit{propagate} and \textit{eliminate} inverse transformations when opportunities to use such results arise.

To summarize, the contributions of this paper include:

- \textit{Szalinski}, a tool that takes a flat CSG expression as input and synthesizes a smaller equivalent program in \textit{Caddy}, a language that extends CSG with map and fold operators for expressing repetition.
- \textit{Inverse transformations}, a new technique for interfacing simple-yet-effective structure finding solvers with E-graphs. The technique is not CAD-specific, but is particularly useful for reordering CAD operations.
- A case study composing Szalinski with a recent mesh decimer [21] to synthesize smaller CAD models.
- A large scale evaluation demonstrating the performance and scalability of Szalinski on models downloaded from a popular online repository [35].

This paper proceeds gradually, first introducing Caddy and a running example (Section 2). Szalinski primarily exploits opportunities to "reroll loops" (Section 3). Finding such opportunities is challenging due to variations in mesh decompiler output (C1), so Szalinski uses E-graphs to implement a robust CAD rewrite system (Section 4). Finding the right CAD reordering is crucial to expose high-level structure (C2), but difficult with rewrites alone due to AC-matching. Solvers in Szalinski propagate profitable reorderings through the E-graph by unifying order-inequivalent expressions annotated with inverse transformations (Section 5).

We developed a library of 65 CAD rewrites and prototyped Szalinski in 3,000 lines of Rust (Section 6). Section 7 shows how composing Szalinski with an existing mesh decompiler [21] qualitatively improves editability (sketched in...
Figure 1) and describes an evaluation of Szalinski’s performance and correctness on real-world CAD models downloaded from Thingiverse. Section 8 briefly surveys the most relevant related work and Section 9 concludes.

2 Caddy and Second Stage Decomposition

The Caddy language (Figure 2) provides map- and fold-like functional list operators to express repetitive structure in CAD models, as well as a Core Caddy fragment that corresponds directly to CSG. The Caddy semantics fully unroll a program’s functional list operators to produce a Core Caddy (CSG) expression. Szalinski “goes the other way,” decompiling a Core Caddy expression to a Caddy program that aims to expose latent repetitive structure. This section introduces a running example that subsequent sections extend to illustrate challenges that arise when shrinking noisy, unstructured outputs from existing mesh decomilers.

2.1 Core Caddy, Caddy, Equivalence

Core Caddy includes various primitives parametrized by dimensions—cuboids parametrized by side length, spheres by radius, cylinders and hexagonal prisms by height and radius, etc. Caddy also provides binary 
set theoretic operators Union, Difference, and Intersection, and affine3 transformations like Translate, Rotate, and Scale that are parameterized by 3D vectors. For example, (Translate [1,0,0] (Sphere 2)) shifts a sphere with radius 2 a single unit of distance along the x-axis. TranslateSpherical (not present in Core Caddy or CSG) captures a common pattern in models relying on translations in spherical rather than Cartesian coordinates.

Figure 3 gives semantics for the functional list operators Caddy provides on top of Core Caddy. Tabulate takes pairs of variables and positive integers (x₁ b₁) . . . (xₙ bₙ) as well as a Caddy expression e, and returns the list of length Πbᵢ generated by n nested loops evaluating e over the variables x₁ . . . xₙ up to the bounds b₁ . . . bₙ:

\[
\text{(List } e[0/x₁] . . . [0/xₙ] . . . e[bₙ − 1/x₁] . . . [bₙ − 1/xₙ])
\]

where e[i/x] denotes substituting all free occurrences (not bound by nested Tabulates) of x in e with i. For example,

\[
\text{(Tabulate (i 2) (j 3) (Cuboid [2 x i + 2. 7. j + 1])) } \Rightarrow \\
\text{(List (Cuboid [2. 7. 1]) (Cuboid [2. 7. 2]) } \text{(Cuboid [2. 7. 3])} \\
\text{(Cuboid [4. 7. 1]) (Cuboid [4. 7. 2]) } \text{(Cuboid [4. 7. 3])})
\]

For the frequent special case of (Tabulate (x n) e) when x is not free in e, we write (Repeat n e) as syntactic sugar.

Map₂ produces a list of Core Caddy expressions by applying an affine operator to a list of transformation parameters and a list of CAD arguments. For example,

\[
\text{(Map₂ affine ps es) } \Rightarrow \text{(List (affine[a₁, b₁, c₁] v₁) (affine[a₂, b₂, c₂] v₂) . . .)}
\]

2.2 A Running Example for Shrinking Caddy

Figure 4a shows a simple CAD model of a ship’s wheel and Figure 4b shows the corresponding desired Caddy output.

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3We use syntactic sugar to present binary nested operators as left-associative over multiple arguments, e.g., (Union a b c) means (Union (Union a b) c).

4Informally, the Hausdorff distance between two meshes is small if every point on one mesh is near some point on the other.
Figure 4. (a) CAD model for a ship’s wheel. (b) Caddy feature like Tabulate express repeated design components. Such repetition can be obvious in Core Caddy (c), but existing mesh compilers obfuscate structure (d).

from Szalinski. Figure 4b reifies repetitive structure: making a change to all the spokes only requires a single edit instead of six coordinated modifications in different locations.

When repetitive structure is easily exposed, as in the ideal Core Caddy of Figure 4c, solvers can infer the arithmetic function relating instances of repeated design components. Section 3 describes Szalinski’s rewrite-driven approach to infer such functions and shrink programs by rerolling loops.

In practice, given a mesh representing Figure 4a, mesh compilers can generate CSG expressions equivalent to Figure 4c, but which obfuscate repetitive structure. Affine transformations may be different or missing and, from a solver’s perspective, lists may be inconveniently ordered or partitioned. Comparing Figure 4c to 4d, Rotate [0,0,180] has been replaced with an equivalent Scale [-1,-1], identity transformations have been omitted, the Union has been reordered, and Scales and Translates have been inconsistently swapped. Sections 4 and 5 walk through progressively more challenging variants of Core Caddy inputs for the ship’s wheel to illustrate how Szalinski uses E-graphs and inverse transformations to robustly handle such variation.

3 Shrinking Caddy by Rerolling Loops
Szalinski shrinks repetitive Caddy programs by “rerolling loops”. First, rewrites find structure by separating affine operators from their parameters and CAD arguments under Map2s. This can expose program repetition as repetitive Lists. Next, arithmetic solvers find equivalent closed form Tabulates for repetitive lists. These Tabulates generalize the program and provide parameters that simplify future edits. Finally, rewrites restore structure by recombining the (generalized) affine parameters and CAD arguments from Map2s into a single Tabulate. Figure 5 shows this strategy’s key rewrites.

Because Szalinski uses an E-graph, these rewrites can actually be repeatedly applied in any order and still efficiently yield the same final result. For simplicity, this section steps through the ship’s wheel example assuming a particular fortuitous order of rewrites that just so happens to nicely shrink the ideal Core Caddy input from Figure 4c.

3.1 Finding Structure: A Bird’s-Eye View
Applying Binop Fold to the inner Union in Figure 4c produces:

\[
\text{(Union (Union (Union (Union ... \langle \text{Fold Union List (List aff List aff)}\rangle \langle \text{Rotate \langle 0,0,0 \rangle \text{cad}_1\rangle}\rangle \langle \text{Rotate \langle 0,0,60 \rangle \text{cad}_2\rangle}\rangle \langle \text{Rotate \langle 0,0,120 \rangle \text{cad}_3\rangle\rangle \langle \text{Rotate \langle 0,0,0 \rangle \text{cad}_4\rangle}\rangle \langle \text{Rotate \langle 0,0,60 \rangle \text{cad}_5\rangle}\rangle \langle \text{Rotate \langle 0,0,120 \rangle \text{cad}_6\rangle\rangle)\rangle)
\]

A structure finder (detailed in Section 4) searches for a list of affine transformations all using the same operator aff. Structure Finding separates the affine parameters and CAD arguments out into two Lists under a Map2 with aff:
Tabulates a specific rewrite order and Figure 4c as an unrealistically
Union the separated affine parameters and CAD arguments to pro-
Repeat over Map2
Finally, since both the
reorder formations allow solvers to
in just the right order. Section 5 shows how inverse transfor-

The structure finder is applied repeatedly. Here it exposes
lists of identical elements, letting the Repeat rewrite produce:

(Fold Union (List (Rotate [0, 0, 0] cad₁) (Map2 Rotate (List [0, 0, 0] [0, 0, 0, 60] [0, 0, 120] ...)) (List [0, 0, 0] [0, 0, 60] [0, 0, 120] ...))
(Fold Union (Map2 Rotate (List [0, 0, 0] [0, 0, 60] [0, 0, 120] ...)) (List cad₁ cad₆ cad₇ ...))

(Fold Union (List (Rotate [0, 0, 0] cad₁) (Map2 Rotate (List [0, 0, 0] [0, 0, 60] [0, 0, 120] ...)) (List [0, 0, 0] [0, 0, 60] [0, 0, 120] ...))
(Fold Union (Map2 Rotate (List [1, −0.5, 0] ...)) (Repeat 6 [1, −0.5, 0])
(Repeat 6 (Cube [10, 1, 1])))

3.2 Introducing Tabulate by Solving Lists
Once structure finding has isolated a List of vectors ℓ, arithmetic
solvers attempt to find equivalent Tabulates. The current
Szalinski prototype provides simple solvers for first- and
second-degree polynomials in both Cartesian and spherical
coordinates. Given ℓ = (List [x₁, y₁, z₁] ... [xₙ, yₙ, zₙ]), these
solvers infer independent functions fₓ, fᵧ, fᶻ for the x, y, z
components of ℓ respectively. In practice, running arithmetic
solvers on floating point numbers output by existing mesh
decomilers requires accepting Tabulates within some ϵ of ℓ,
especially for tools that rely on randomized algorithms [11]
like RANSAC [28].

For the Rotate parameters (List [0, 0, 0] [0, 0, 60] ... [0, 0, 300]),
solvers find (Tabulate (i 6) [0, 0, 60i]). List Solve then produces:

(Fold Union (Map2 Rotate (List [0, 0, 0] [0, 0, 60] [0, 0, 120] ...) (List [0, 0, 0] [0, 0, 60] [0, 0, 120] ...))
(Map2 Translate (Repeat 6 [1, −0.5, 0]) (Repeat 6 (Cube [10, 1, 1])))

In this example, the solvers relied on their input arriving
in just the right order. Section 5 shows how inverse transfor-
amations allow solvers to reorder their input to infer better
Tabulates while preserving equivalence.

3.3 The Final Squeeze: Recombining Map2s
Finally, since both the Repeats and Tabulate have matching
bounds, Repeat over Map2 and Tabulate over Map2 recombine
the separated affine parameters and CAD arguments to pro-
duce the desired output from the inner Union of Figure 4c:

(Fold Union (Map2 Rotate (Tabulate (i 6) [0, 0, 60i]) (Map2 Rotate (Translate [1, −0.5, 0] (Cube [10, 1, 1])))
(Map2 Translate (Repeat 6 [1, −0.5, 0]) (Repeat 6 (Cube [10, 1, 1])))
(Repeat 6 (Cube [10, 1, 1])))

This section illustrated Szalinski’s core strategy: shrinking
Caddy by rerolling loops. However, the example relied on
a specific rewrite order and Figure 4c as an unrealistically
ideal input. Subsequent sections show how E-graphs and
inverse transformations enable Szalinski to robustly shrink
noisy and unstructured CSGs.

4 E-graphs and CAD Equality Saturation
Rewrites to shrink Caddy by rerolling loops must be applied
in just the right order to programs that already make structure
apparent as in Figure 4c. Simply interleaving additional
CAD rewrites to expose repetitive structure initially seems
infeasible because the necessary rewrites are not confluent and
the space of possible orderings explodes exponentially. However,
past work on Equality Saturation [34] demonstrates how
E-graphs [22] can make this strategy efficient for many
rewrite rules. This section shows how Szalinski applies Equality
Saturation in the CAD domain to robustly handle CSG
variations when shrinking Caddy programs.

4.1 Rewrite Phase Ordering: What, When, Where
A slightly perturbed Caddy example for the spokes of the
ship’s wheel omits Rotate [0, 0, 0] and replaces Rotate [0, 0, 180]
by the equivalent Scale [−1, −1, 1]:

(Fold Union (List (Rotate [0, 0, 0] (Translate [1, −0.5, 0] (Cube [10, 1, 1])))
(Rotate [0, 0, 120] (Translate [1, −0.5, 0] (Cube [10, 1, 1])))
(Scale [−1, −1, 1] (Translate [1, −0.5, 0] (Cube [10, 1, 1])))
(Rotate [0, 0, 240] (Translate [1, −0.5, 0] (Cube [10, 1, 1])))
(Rotate [0, 0, 300] (Translate [1, −0.5, 0] (Cube [10, 1, 1])))

The three-phase loop rerolling strategy from Section 3
now breaks: Szalinski must interleave its search with additional
CAD rewrites (Figure 6) to expose the repeated affine
transformations as in Figure 4c. This phase ordering prob-
lem [34, 38] makes it difficult to determine when to apply
which rewrites and where. Poor choices will only further
obfuscate repetitive structure and no single strategy is best
in general.

Equality Saturation [34] is a technique to mitigate phase
ordering that uses E-graphs to compactly represent equiva-
lence relations over large sets of expressions. Instead of
destructively modifying a particular concrete term, rewrites
extend the E-graph by adding and unifying classes of ex-
pressions. This eliminates the need to choose any particular
rewrite ordering. By repeatedly applying the rules in Fig-
ures 5 and 6 to an E-graph and using a structure finding
heuristic (Section 4.4), Szalinski’s loop rerolling strategy can
robustly handle variations in how mesh decomilers synthe-
size affine operators.

4.2 E-graph Background
An E-graph is a set of ecllasses, and each eclass is a set of
equivalent enodes. An enode is an operator (Translate, Union,
literal, etc.) applied to zero or more child ecllasses. An eclass e
represents expression e if e contains an enode n with the same
operator as e and the children of n represent the children of e.
Affine Identities

- (Rotate \( [0, 0, 180] \) cad) \( \leftrightarrow \) (Scale \([-1, -1, 1]\) cad)
- (Rotate \( [0, 0, 0] \) cad) \( \leftrightarrow \) cad
- (Translate \( [0, 0, 0] \) cad) \( \leftrightarrow \) cad
- (Scale \( [1, 1, 1] \) cad) \( \leftrightarrow \) cad

Affine Interchanging

- (Scale \( [a, b, c] \)) \( \leftrightarrow \) (Translate \( [d, e, f] \) cad)
- (Translate \( [a, b, c] \)) \( \leftrightarrow \) (Translate \( [d, e, f] \) cad)

Affine Combination

- (Scale \( [a, b, c] \)) \( \rightarrow \) (Scale \( [a d, b e, c f] \) cad)
- (Translate \( [a, b, c] \)) \( \rightarrow \) (Translate \( [a + d, b + e, c + f] \) cad)

Primitive-Affine Conversion

- (Cube \( [x, y, z] \)) \( \leftrightarrow \) (Scale \( [r, r, r] \) (Sphere 1))
- (Sphere \( r \)) \( \leftrightarrow \) (Scale \( [r, r] \) (Sphere 1))
- (Cylinder \( [h, r] \)) \( \leftrightarrow \) (Scale \( [r, h] \) (Cylinder 1))
- (Hex prism \( [h, r] \)) \( \leftrightarrow \) (Scale \( [r, r, h] \) (Hex prism 1))

Figure 6. Selected CAD identities. Bidirectional arrows indicate Szalinski has a rule for each direction.

![Figure 6](image)

Each eclass represents an exponential number of equivalent expressions (w.r.t. the number of enodes), since each of its enodes point to eclosures themselves.

Adding an expression to an E-graph works bottom up: first add the leaves as enodes each in their own eclosures, then recursively add operators as enodes pointing to the eclosures of their operands as children. Hashcasing ensures enodes are never duplicated in an E-graph. This sharing compactly represents many equivalent expressions.

E-graphs also provide a unify operation that combines two eclosures and maintains their congruence closure. For example, if eclosures \( c_1 \) and \( c_2 \) represent \((x + y)\) and \((x + z)\) respectively, then unifying the eclosures representing \( y \) and \( z \) would cause \( c_1 \) and \( c_2 \) to be unified as well since they both contain "+" enodes with equivalent children. Figure 7 shows how an E-graph can compactly represent equivalent expressions generated by rewrites, in this case, one of the CAD rewrites needed to expose repetitive structure for the ship’s wheel example.

E-graphs can easily be extended with syntactic rewrites \( a \rightarrow b \): whenever an eclass \( c \) represents an expression that matches pattern \( a \) under substitution \( \phi \), the eclass representing \( \phi(b) \) is found (or constructed) and unified with \( c \); the resulting eclosure will represent both expressions \( \phi(a) \) and \( \phi(b) \). Rewrites only expand the E-graph, all previous expressions are still represented.

We slightly generalize rewrites from two patterns to a pattern \( L \) and a function \( R \) that, given a substitution \( \phi \), returns an expression to be added to the E-graph and unified with the eclosure that matched \( L \). This generalization allows rewrites to implement rules which are not purely syntactic, like constant folding (ex: rewriting \( 2 + 3 \) to 5). Many of Szalinski’s list-manipulating rewrites are implemented this way, which is convenient for rules like Repeat which need to extract the length of a matched list pattern. This generalization also allows Szalinski to integrate arithmetic solvers with the E-graph—Tabulate expressions returned by solvers are unified with the eclass that matched the List Solve rule’s list pattern.

4.3 Equality Saturation in Szalinski

Szalinski implements Equality Saturation [34] for Caddy (Figure 8). First, an E-graph is created from the input Core Caddy expression. Then Szalinski expands the E-graph by repeatedly applying rewrites. Searching the E-graph for a rewrite’s left-hand side pattern results in a list of (eclass, substitution) pairs that indicate where and how a pattern was matched. For each pair \((c, \phi)\), Szalinski generates an expression \( e \) by applying the rewrite’s right-hand side function to \( \phi \), adding \( e \) to the E-graph yielding eclass \( c’ \), and unifying \( c \) and \( c’ \). Szalinski continues applying rewrites until the E-graph saturates (reaches a fixpoint where no rewrites further expand the E-graph), or a timeout is reached. In the case of saturation, Szalinski has discovered all equivalences derivable from its rewrites.

```python
def Szalinski(csg : core_caddy):
    egraph, root = make_egeraph(csg)
    while egraph.changed():
        for (lhs, rhs) in SZALINSKI_REWRITES:
            matches = egraph.search(lhs)
            for (eclass, subst) in matches:
                c = egraph.add(apply(rhs, subst))
                egraph.unify(eclass, c)
    return egraph.extract(root, min_size)
```

Figure 8. Equality Saturation for Caddy in Szalinski

![Figure 8](image)
Finally, Szalinski extracts the smallest Caddy program represented by the initial Core Caddy input’s eclass in a simple bottom-up traversal of the E-graph. Szalinski uses program size as a proxy for editability. Past work provides extraction strategies for various kinds of cost functions [24, 34], but we leave further exploration of CAD cost functions in Szalinski to future work.

4.4 Structure Finding in E-graphs

Since Szalinski’s rewrites contain CAD identities that can fire in every iteration, the structure finding procedure as presented in Section 3.1 must be enhanced. It must consider that multiple affine transformations may be introduced in the same eclass by the CAD identities. Given a list of eclasses \(e_1, e_2, \ldots, e_n\), the structure finder aims to extract Map2s that remove one level of structure. However, due to rules like Affine Combination from Figure 6, each eclass may contain multiple equivalent enodes with the same affine operation. If eclass \(e_i\) has two enodes with the Rotate operator, for example, the structure finder can choose from 2 different Rotates at each of the \(n\) eclasses in the list. Each of these \(2^n\) Map2s has distinct children, and will therefore be a distinct enode in the E-graph, all unified in the same eclass as the list itself. Szalinski must operate on large lists of Core Caddy programs, but such an exponential number of enodes would blow up the E-graph.

Szalinski instead capitalizes on the observation that it is not useful to pick different affine enodes within similar-looking eclasses. Consider again the ship’s wheel example presented in Section 4.1. After applying the two Rotate identities from Figure 6, the eclasses for the top-level affines in the list contain the following enodes (one eclass per row, enodes shown with their parameters for clarity):

\[
\begin{align*}
\text{a:} & \quad (\text{Translate} \ [1,-0.5,0]) \ (x_1) & \quad (\text{Rotate} \ [0,0,0]) \ (a) \\
\text{b:} & \quad (\text{Rotate} \ [0,0,0]) \ (x_2) & \quad (\text{Rotate} \ [0,0,0]) \ (b) \\
\text{c:} & \quad (\text{Rotate} \ [0,0,0]) \ (x_3) & \quad (\text{Rotate} \ [0,0,0]) \ (c) \\
\text{d:} & \quad (\text{Scale} \ [1,-1,1]) \ (x_1) & \quad (\text{Rotate} \ [0,0,0]) \ (d) & \quad (\text{Rotate} \ [0,0,0]) \ (x_4) \\
\text{e:} & \quad (\text{Rotate} \ [0,0,0]) \ (x_2) & \quad (\text{Rotate} \ [0,0,0]) \ (e) \\
\text{f:} & \quad (\text{Rotate} \ [0,0,0]) \ (x_3) & \quad (\text{Rotate} \ [0,0,0]) \ (f)
\end{align*}
\]

The structure finder calculates the affine signature of each eclass as the multiset of the kinds affine operators in the eclass. In the above example, eclass \(a\)'s affine signature is \{Translate, Rotate\}, \(d\)'s is \{Scale, Rotate, Rotate\}, and the others all share the same signature: \{Rotate, Rotate\}. A group is a set of eclasses that share the same affine signature. When trying to extract a Rotate, the structure finder will not take the Cartesian product of the Rotates in each eclass—doing so would lead to \(2^5\) possible ways to combine Rotate. Instead, it takes the Cartesian product of affine choices for each group, and extends the same choice of affine over all eclasses within the group (using the order of affines in the eclasses). In this example, the only affine that can be extracted is Rotate, since the other affines do not appear in the affine signature of all groups. For the Rotate affine, group \(a\) has one choice, group \(\{(\text{Fold }, \text{Union }, \text{List}) \ (\text{Rotate} \ [0,0,120]) \ (\text{Translate} \ [1,-0.5,0]) \ (\text{Cuboid} \ [10,1,1]) \}

\]

Figure 9. Section 3 and 4 techniques find the "Rotate then Translate" structure from the realistic Figure 4d. Without inverse transformations, loop rerolling now gets stuck.

\[d\] has 2 choices, and group \(b, c, e, f\) also has 2 choices. This reduces the number of \((\text{Map2 } \text{Rotate} \ldots)\) expressions introduced from \(2^5 = 32\) to 4.

5 Inverse Transformations

E-graphs and CAD rewrites allow Szalinski to expose repetitive structure and reroll loops even when a Core Caddy input exhibits obfuscating variations (e.g., \(\text{Scale} \ [-1,-1,1]\) instead of \(\text{Rotate} \ [0,0,180]\)). However, existing mesh decoders tend to also order and group CAD subexpressions by geometric proximity or other heuristics that, from Szalinski’s perspective, make recovering high-level structure challenging. Unless the right reordering and regrouping of subexpressions can be found, list solvers will fail to infer Tabulates and Szalinski will be unable to reroll loops and shrink Caddy programs.

To address this challenge, we introduce inverse transformations, a novel way for solvers to optimistically unify expressions in an E-graph that would be equivalent modulo reordering or regrouping. Figure 9 shows how far CAD rewrites combined with techniques from previous sections get for the Figure 4d example. Unfortunately, Cylinder is still Unioned with Cuboids, preventing the structure finder from pulling out the Rotate. Even if the Cylinder were removed, the list order would prevent solvers from inferring a Tabulate for the Rotate parameters. Unlike the previous section, adding more rewrites does not help.\(^5\) E-graphs do not compactly represent equivalences due to reordering associative and commutative operators like Union. This is known as the AC-matching problem [3] (A stands for associativity, and C for commutativity) and it prevents efficiently exploring all possible reorderings and regroupings.

Szalinski addresses this with a new technique, inverse transformations, that allows solvers to speculatively transform their inputs to allow for more profitable rewriting. A solver that cannot simplify input \(A\) may, for some transformation \(F\), be able simplify \(F(A)\) to \(B\). Inverse transformations simply allows the solver to "wrap" \(B\) with \(F^{-1}\) before unifying it with \(A\), even though \(A\) and \(B\) are not equivalent.

\(^5\)We can report that AC-matching is a problem both in theory and practice.
permutation ::= ( n, n, ... )  partitioning ::= ( n, n, ... )

inv ::= (Sort (permutation) (\^\-list)) 
| (Unsort (permutation) (\^\-list)) 
| (Part (partitioning) (\^\-list)) 
| (Unpart (partitioning) (\^\-list)) 
| (Spherical (vec3) (vec3\-list)) 
| (Unspherical (vec3) (vec3\-list))

**Figure 10.** Syntax of Extended Caddy.

Inverse transformations enable locally-reasoning solvers to register potentially profitable regroupings and reorderings in an E-graph. Simple syntactic rewrite then propagate these “hints” globally through the E-graph, allowing other solvers to try them, and contextually eliminate inverse transformations when possible (e.g., under order-insensitive operations like Fold Union).

### 5.1 Extended Caddy

Extended Caddy (Figure 10 and 11) adds inverse transformations that allow solvers to record how they manipulated their input. These extended forms are only introduced in the E-graph; Szalinski’s cost function ensures extraction produces regular Caddy programs. Semantically, these constructs either undo the transformation performed by the solver to recover the input, or perform the transformation on some other part of the program. Sort and Unsort take a permutation \( p \) and a list \( \ell \), imposing (respectively, undoing) \( p \) on \( \ell \). Part takes a partitioning \( P \) (a list of lengths) and a list \( \ell \), breaking down \( \ell \) into a list of sublists according to \( P \). Unpart takes a partitioning and a list of lists and flattens the latter; the partitioning is only used to propagate information. TranslateSpherical and UnsphereSpherical take a 3D vector \( c \) and a list of 3D vectors in spherical coordinates about \( c \), returning a list of the vectors in Cartesian coordinates (and vice versa).

### 5.2 Restructuring with Unpart and Unsort

Using inverse transformations, Szalinski can finally get the desired output given the realistic input for the ship's wheel (Figure 4d). Starting from Figure 9, Szalinski separates the Cylinder from the Cuboids with partitioning and sorts the list of Cuboids on their Rotate parameters, revealing repetitive structure similar to the ideal input (Figure 4c).

**Partitioning.** Szalinski includes a partitioning solver that uses inverse transformations and a set of heuristics to restructure lists in ways that group similar list elements together (e.g., by kind of geometric primitive). The partitioner can split up elements of a list by equivalence class, individual components of 3D vectors, and kinds of affine transformations. In Figure 9, the partitioner will split the list into:

(Fold Union 
(Unpart (1, 6) 
(List (Cylinder [1, 5])))

| e ⇒ (List v₁ v₂ ... vₙ) |
| (Sort (l₁, l₂, ..., lₙ) e)⇒ (List v₁, v₂, ..., vₙ) |
| e ⇒ (List v₁, v₂, ..., vₙ) |
| (Unsort (l₁, l₂, ..., lₙ) e)⇒ (List v₁, v₂, ..., vₙ) |

| (Spherical (vec3) (vec3\-list)) |
| (Unspherical (vec3) (vec3\-list)) |

**Figure 11.** Big step semantics for Extended Caddy.

The introduced Unpart is equivalent to Concat, but additionally stores partitioning hints. Now that the Rotates are gathered uniformly in a list, the structure finder will rewrite the list to:

(Map2 Rotate 
(List [0, 0, 120] (Translate [1, 0, 0] (Cuboid [10, 1, 1])) 
(List [0, 0, 120] (Translate [1, 0, 0] (Cuboid [10, 1, 1])) 
(List [0, 0, 300] (Translate [1, 0, 0] (Cuboid [10, 1, 1])) 
(List [0, 0, 180] (Translate [1, 0, 0] (Cuboid [10, 1, 1])) 
(List [0, 0, 240] (Translate [1, 0, 0] (Cuboid [10, 1, 1])) 
(List [0, 0, 60] (Translate [1, 0, 0] (Cuboid [10, 1, 1])))

The arithmetic solver from Section 3.2 cannot find a closed form for this list of Rotate parameters. The solver could, however, find a closed form if it were free to sort the list (by \( z \)-coordinate, in this case). The sorted list is not equivalent to the original. Since the solver only rewrites locally, it does not know if the list appears under a Fold Union (which is AC) or a Fold Diff (which is not AC). In the E-graph, both situations could actually hold due to sharing. The solver cannot soundly rewrite the original list to the closed form Tabulate, but it can soundly rewrite the list to:

(Unsort (1, 5, 0, 3, 4, 2) (Tabulate (6) [0, 0, 60]))

The Unsort inverse transformation allows the solver to introduce the closed form Tabulate in the E-graph, but Szalinski will never extract it or any other program using the inverse transformation forms from Extended Caddy. Instead, rewrites propagate inverse transformations between invocations of locally-reasoning solvers, and additional rules eliminate inverse transformations in contexts invariant to
the relevant transformation; these rules are shown in Figure 12. The Map2 Unsort Params rewrite applies to our running example, producing:

\[(\text{Unsort} \ (1, 5, 0, 3, 4, 2)) (\text{Sort} \ (1, 5, 0, 3, 4, 2))\]

\[(\text{Map2 Rotate})\]

\[(\text{Unsort} \ (1, 5, 0, 3, 4, 2) (\text{Tabulate} \ ([i \ 6]) [0, 0, 6i]))\]

\[(\text{Repeat} \ 6 \ (\text{Translate} \ [1, -0.5, 0] \ (\text{Cuboid} \ [10, 1, 1])))\]

Semantically, this is no different, as \((\text{Unsort} \ p \ (\text{Sort} \ p \ x)) = x\), but since the Map2 is in the same eclass as the original list of Rotates, the Sort Application rule can fire, communicating the profitable ordering of the Rotate parameters to the outer list. Now, the structure finder and arithmetic solver apply to the sorted list of Rotates, bringing the whole program to:

\[(\text{Fold Union}) \]

\[(\text{Unpart} \ (1, 6))\]

\[(\text{List} \ (\text{Cylinder} \ [1, 5]))\]

\[(\text{Unsort} \ (1, 5, 0, 3, 4, 2))\]

\[(\text{Tabulate} \ (i \ 6))\]

\[(\text{Rotate} \ [0, 0, 6i])\]

\[(\text{Translate} \ [1, -0.5, 0])\]

\[\text{Cuboid} \ (10, 1, 1)\]

From here an additional rewrite (elided from Figure 12) can lift the Unsort over the Unpart:

\[(\text{Fold Union})\]

\[(\text{Unsort} \ (0, 2, 6, 1, 4, 5, 3))\]

\[(\text{Unpart} \ (1, 6))\]

\[(\text{List} \ (\text{Cylinder} \ [1, 5]))\]

\[(\text{Tabulate} \ (i \ 6))\]

\[(\text{Rotate} \ [0, 0, 6i])\]

\[(\text{Translate} \ [1, -0.5, 0])\]

\[\text{Cuboid} \ (10, 1, 1)\]

Next, the Unsort Elimination rule removes the Unsort, since Fold Union is invariant to order. Finally one additional rule that transforms a Union of an Unpart into a Union of Unions (not shown), produces the desired Caddy output (Figure 4b).

5.3 Solving for Spherical Coordinates

Inverse transformations are not restricted to list manipulations. In addition to sorting, Szalinski’s arithmetic solvers can convert lists to spherical coordinates [19]. The resulting list may be easier to find a closed form Tabulate for, but it is not equivalent to the input. Therefore, the solver wraps the Tabulate in an inverse transformation, Un spherical, before passing it to the E-graph for unification. If the Un spherical propagates under a Translate, then the Un spherical Trans rule can replace it with TranslateSpherical form. This approach allows Szalinski to solve for closed forms of lists in spherical coordinates without the solver knowing whether or not it is solving for a list of Translate parameters.

5.4 Inverse Transformations, Broadly

This section and our evaluation show that inverse transformations are effective for shrinking Caddy programs, but the technique could be applied more broadly to other uses of Equality Saturation. The key insight is that solvers can remain simple because they only have to reason locally. They are given the flexibility to speculate on potentially profitable ways to transform their inputs. Rewrites can then propagate this information and contextually eliminate the transformations. As in traditional Equality Saturation, these rewrites (and now simple solvers) compose in emergent ways, leading to unexpectedly powerful outcomes, that would have otherwise required more complicated solvers with deep, contextual reasoning ability.

6 Implementation

Szalinski is implemented in 3000 lines of Rust and uses egg [41], an open source E-graph library. Table 1 provides a break down of the LOC for each of Szalinski’s components. Szalinski uses only simple, custom solvers for arithmetic and list partitioning. The most of Szalinski’s 65 rewrites are syntactic and compactly expressed, and the remainder either call out to the solvers or manipulate lists. Szalinski is publicly available at https://github.com/uwplse/szalinski.git.

<table>
<thead>
<tr>
<th>Caddy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rewrites</td>
</tr>
<tr>
<td>Solvers</td>
</tr>
<tr>
<td>Main loop</td>
</tr>
<tr>
<td>Validation</td>
</tr>
<tr>
<td>300</td>
</tr>
<tr>
<td>900</td>
</tr>
<tr>
<td>400</td>
</tr>
<tr>
<td>300</td>
</tr>
<tr>
<td>1100</td>
</tr>
</tbody>
</table>
We then use the CGAL [4] library to compute the Hausdorff distance with 32 GB of RAM. To evaluate the composability of Szalinski with mesh decomposition tools, we ran Reincarnate on their mesh files to get flat CSGs and their core Caddy, converted those to Core Caddy. We found 10 such models from Thingiverse [35] and ran Reincarnate on their mesh files to get flat CSGs and converted those to Core Caddy.

Correctness. To validate Szalinski’s correctness, we test that the initial and final Caddy programs compile to similar meshes (Figure 13). Szalinski first evaluates a Caddy program back to a flat Core Caddy program which is then pretty printed to a CSG program. We use the open source OpenSCAD [23] tool to compile the CSGs to triangular meshes. We then use the CGAL [4] library to compute the Hausdorff distance [11, 20] between the two meshes. A Hausdorff distance less than a small $\epsilon$ indicates equivalence (ideally it should be zero, but due to rounding errors, it is sufficient to check against $\epsilon$).

7 Evaluation

In evaluating Szalinski, we were interested in the following research questions:

- **End-to-End.** (Section 7.1) Does Szalinski compose with prior mesh decomposition tools and find parameterizable programs from the flat CSG expressions generated by the latter?
- **Scalability.** (Section 7.2) Does Szalinski scale to large flat CSGs? How fast can it find equivalent smaller Caddy programs?
- **Sensitivity analysis.** How do the different components of Szalinski, in particular CAD rewrites and inverse transformations, affect its results?

We ran our evaluation on a 6 core Intel i7-8700K processor with 32 GB of RAM.

7.1 End-to-End Experiments

To evaluate the composability of Szalinski with mesh decomposition tools, we ran Szalinski on flat CSGs generated by the Reincarnate [21] mesh decompiler. This required investigating what kinds of models Reincarnate supports; we found that it worked best on models that do not contain round edges. We found 10 such models from Thingiverse [35] and ran Reincarnate on their mesh files to get flat CSGs and converted those to Core Caddy.

Given the Core Caddy inputs, Szalinski synthesizes Caddy programs (Figure 13). We compared the parameterized programs synthesized by Szalinski from Reincarnate’s output with manually written parametrized programs in OpenSCAD (column 1 in Table 2). For four of the 10 models, we found a parametrized OpenSCAD implementation on Thingiverse. For the other six, we manually wrote a parametrized implementation in OpenSCAD. Table 2 shows the comparison of the lines of code at every stage of the end-to-end synthesis process, and the cost of the flat input Core Caddy and the output Caddy. Szalinski was able to reduce the cost of the programs by 86% on average. The last two columns report a sensitivity analysis of Szalinski on Reincarnate’s output. It shows that both CAD identities and inverse transformations contribute significantly to shrinking Caddy programs.

Compiling the Caddy programs to mesh resulted in meshes equivalent to the source meshes (Hausdorff distance $< 0.001$). We also manually validated that all 10 inferred Caddy programs are structurally similar to the parameterized input OpenSCAD programs.

7.2 Large Scale Evaluation on Thingiverse Models

Mesh decomposition tools have limitations. Reincarnate for example, works mainly on shapes without rounded corners and edges. Therefore, in order to evaluate Szalinski further, we performed a large scale evaluation on models from Thingiverse [35], a popular online model sharing website.

The goals for this part of the evaluation are: (1) to simulate the behavior of mesh decomposition tools by flattening parameterized programs and perturbing them to reproduce the challenges (C1) and (C2) (introduced in Section 1), and run Szalinski on these flat CSGs, (2) to analyze the scalability,
correctness and efficiency of Szalinski on large-scale real world programs.

Data Collection. We built a scraper that downloaded customizable models from Thingiverse. While most models in Thingiverse are shared as triangular meshes which are hard to customize, models under the "Customizable" category [7] are intended to be editable, and are therefore more likely to be accompanied with higher-level programmatic representation. Our scraper found 12,939 OpenSCAD files from the "Customizable". 912 of these files were invalid, i.e. they were empty, could not be compiled, or used debug features. We filtered out files using features we do not support (like linear extrusion), leaving 2,127 models. Similar to Caddy, the OpenSCAD language supports CSG and also has features like for loops that can be used to write more parametrizable CAD programs. OpenSCAD can compile these programs to flat CSG, which Szalinski then accepts as input. Figure 14 summarizes the AST sizes of these inputs.

OpenSCAD primitives like spheres and cylinders are parameterized by their geometric precision. The geometric precision indicates the quality of the mesh obtained when the CSG is compiled. For example, a sphere with resolution 100 has a more fine-grained mesh than a sphere with resolution 10. We found several examples where the precision of the primitives was as high as 100. However, OpenSCAD’s compiler is slower when generating finer resolution meshes. Since our verifier (Section 6) uses the OpenSCAD compiler, we capped the precision of all primitives to 25.

Results. Figure 15 shows our results with a 60 second timeout. We refer to the baseline result (leftmost) as slightly perturbed, as OpenSCAD represents affine transformations in an ambiguous way in its CSG format (ex: the representation of Scale [-1,-1,1] and Rotate [0,0,180] are identical). The second result shows that Szalinski is fast; limiting it to 1 second has very little effect on the result. The third result shows Szalinski is robust to reordering of the inputs. The final two results show CAD rewrites or inverse transformations significantly contribute to Szalinski’s performance. We validated all results with the by comparing the meshes. All Hausdorff distances were under 0.01, except for 148 cases where CGAL failed to compute the distance and we visually compared the meshes.

7.3 Case Studies and Editability

This section discusses three models from the end-to-end evaluation in Section 7.1 (a fourth is illustrated in Figure 1) and three models from the large scale evaluation in Section 7.2. The goal is to highlight some edits made easily possible by Szalinski, which in the flat CSG (and mesh) are nearly impossible. Figure 16 shows a rendering of these models and the parametrized Caddy program found by Szalinski. We discuss three categories of edits.

Adding or removing components: consider the gear shown in Figure 16. Changing the tooth count in a flat CSG version of this model requires manually computing the position of every teeth and ensuring that the spacing between them is still equal. The Caddy program synthesized by Szalinski makes this modification trivial—it exposes a function (6 × i) for Rotate and the number of teeth (in the Tabulate), which can both be easily changed to get a different tooth count. Adding rows or columns of components is also easy in a parametrized model. For example, in the first model in Figure 16, another set of compartments can be added by changing the bounds of Tabulate.

Modifying the shape of multiple components: in the last model in Figure 16, the cylinders can be all changed to Hexprism by changing it in two places only. These modifications in the flat CSGs require changing the shape of each cylinder individually, which is undesirable. Figure 1 shows more examples of edits where the shape of the hex-wrench holder can be changed by changing the parameters inferred by Szalinski.

Applying additional affine transformations to components: consider the SD card rack (the second model) in Figure 16. This model can be easily customized in the Caddy program to adjust the size of the slots. The Caddy program in the figure shows that in each iteration (in Tabulate), two sizes of Cuboid are removed from the outer box. The dimensions of these can be changed in the function inferred for the Cuboid parameters: (Cuboid [4.5, 25, j + 0.5]) to change the slot size. Similarly, Figure 1 showed how an additional rotation can be easily added to Cuboid to make an entirely different model.

Performing these modifications in a flat CSG is tedious and error-prone because they require manually recomputing
Figure 15. Result of running Szalinski on 2,127 Thingiverse examples. Models are grouped by AST size of initial Core Caddy input: 769 were tiny (AST size < 30), 786 small (30 < size < 100), 374 medium (100 < size < 300), and 198 large (300 < size).

Figure 16. The first three are examples of end-to-end evaluation where Szalinski ran on the flat CSG output of a mesh decompiler [21]. The last three are representative examples that show the usefulness of Szalinski where the flat CSG was generated using OpenSCAD and perturbed to simulate mesh decoders.

many parameters for multiple components in the models. Szalinski makes these modifications much easier by exposing different design parameters.

7.4 Limitations
Some mesh decomposition tools like InverseCSG synthesize flat CSG programs using enumerative synthesis and random sampling based algorithms like RANSAC [11]. Inferring structure from the output generated by these tools requires equivalence under context using geometric reasoning that our prototype currently does not support. InverseCSG provides 50 benchmarks, on all of which we ran Szalinski. The majority of the benchmarks lacked the repetitive structure Szalinski is intended to infer. For one of the models (benchmark 157, a gear), Szalinski was able to infer a TranslateSpherical function. However, due to the structure of their outputs, we had to add rewrites like:

\[(\text{Difference}(\text{Union} \ a \ b \ c)) \rightarrow (\text{Union}(\text{Difference} \ a \ c) \ b)\]

which are unsound without a geometric solver that can check that the intersection of \(b\) and \(c\) is empty. We manually applied this rewrite to benchmark-157 but did not add these rewrites to Szalinski’s rule database due to their unsoundness.

8 Related Work
E-graph based Deductive Program Synthesis. E-graphs have been used extensively in superoptimizers [2, 16, 33, 34], and SMT solvers [8–10, 37]. Szalinski’s core algorithm is a generalized version of equality saturation [34]. Integrating linear solvers with compiler optimizers has a long history with tools like Omega Calculator [25, 26]. Our approach of using syntactic rewrites and an arithmetic function solver to modify the E-graph can be considered similar to Simplify [10] which uses an E-graph module for finding equivalent expressions containing uninterpreted functions, and a Simplex module that is used for arithmetic computations.

However, unlike Szalinski, past work does not allow solvers to speculatively add potentially profitable expressions in the E-graph. Inverse transformations allows Szalinski to accomplish this while also mitigating the AC-matching problem for...
associative and commutative operations like list reordering and regrouping.

**2D and 3D Design Synthesis.** Nandi et al. [21] and Du et al. [11] have developed tools that can decompile low-level polygon meshes to flat CSGs. These tools use program synthesis together with domain-specific computational geometric algorithms to discover structure in the meshes. CS-GNet [30] uses machine learning to generate flat CSG programs for 2D and 3D shapes. Shape2Prog [36] uses machine learning to infer programs from voxel-based 3D models. They use LSTMs to infer programs with loops. We ran Szalinski on the flat CSGs from both CS-GNet and Shape2Prog—since their program lengths are very small (AST depth < 7), they are not good candidates for design parameter inference. Szalinski however did find some structure in these program and generated correct outputs. Ellis et al. [13] developed a tool that can automatically generate programs that correspond to hand-drawn images. They first use machine learning to detect primitives in the drawings and then use Sketch [32] to find loops and conditionals. Szalinski’s technique is different from theirs in that they use enumerative search to explore all programs within a given depth (their max AST depth is 9), based on a language grammar, a specification, and a cost, whereas Szalinski uses a rewrite-based synthesis technique where the specification is given as the initial CSG, and Szalinski constructs an E-graph and updates it using semantics preserving rewrites. In order to compare Szalinski with Ellis et al.’s [13] tool, we ported their 2D models to 3D and ran Szalinski on them. Szalinski’s results had similar loop structure as theirs but further comparison is not possible since their DSL is different. Another line of work [12] uses reinforcement learning to synthesize programs for 2D and 3D models. However, the programs inferred by these approaches are much smaller compared to Szalinski.

In computer graphics and vision, symmetry detection [18] in 3D shapes is a well studied topic. It can improve performance of geometry processing algorithms. The ability to detect folds and maps in 3D models is more general than symmetry detection because it can find patterns in models that have repetitive structure that is not symmetry. A simple example of this is a union of \( n \) cubes increasing in size. In fabrication, Schulz et al. [29] developed algorithms for optimizing parametric CAD models using interpolation methods. While their approach can optimize parameters, it does not automatically infer maps and folds from flat CSG inputs.

9 Conclusion

This paper addresses the challenge of synthesizing smaller high-level CAD models from the noisy and unstructured outputs of existing triangle mesh to CSG decompilers. We developed **Szalinski**, a prototype tool to synthesize **Caddy** programs using semantics-preserving rewrites and simple solvers to “reroll loops.” By adapting Equality Saturation to the CAD domain, Szalinski can robustly handle common CSG variations exhibited by existing mesh decompilers. Szalinski relies on novel **inverse transformations** to mitigate the AC-matching problem that arises when reordering CAD operations: solvers annotate and merge terms that are only equivalent modulo reordering, then propagate and eliminate such annotations through an E-graph to expose repetitive structure and robustly enable loop rerolling. Inverse transformations are not CAD-specific: we are excited to explore future work investigating how they may be applied in other ordering-sensitive optimization problems, e.g., instruction scheduling [39, 40].

To the best of our knowledge, Szalinski is the first tool of its kind. We performed an early survey of 2,127 real-world CAD models from Thingiverse. Our evaluation shows that Szalinski can dramatically shrink many CAD models in seconds.

In future work, we are excited to explore richer rewrites for contextual equivalence (Section 7.4), more expressive cost functions for capturing richer notions of editability, and connections to interactive CAD editing using direct manipulation tools like Sketch-n-Sketch [5].

Acknowledgments

We thank René Just for valuable suggestions on data visualization, and other members of the UWPLSE lab for feedback on early drafts. We also thank our shepherd, Mukund Ragho-taman, and the anonymous reviewers for their guidance while preparing the final revision of this paper. This material is based upon work supported by the National Science Foundation under Grant No. CCF-1813166.

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